

# Probing New Physics with MeV Telescopes

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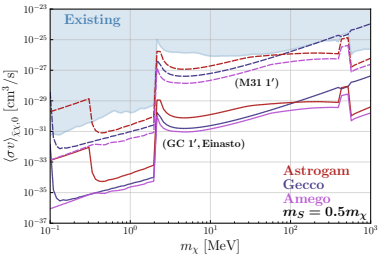


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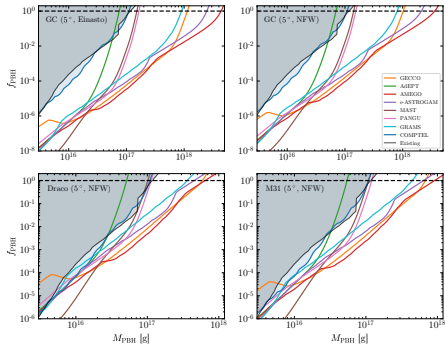
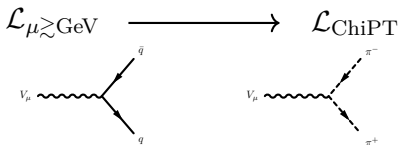
# Preview

- Dark matter with  $m_\chi < \text{GeV}$  is an exciting prospect
- Exciting upcoming MeV  $\gamma$ -ray telescopes could probe the dark sector to unprecedented sensitivity
- New tools developed explicitly for studying MeV physics

# Preview



# Dictionary



# Overview

- 1 Motivation
- 2 MeV Dark Matter
- 3 Primordial Black Holes
- 4 Future Work
- 5 Conclusions

# Why MeV Dark Matter?

# Motivation

- ① For decades, WIMPs have been the de facto DM candidates

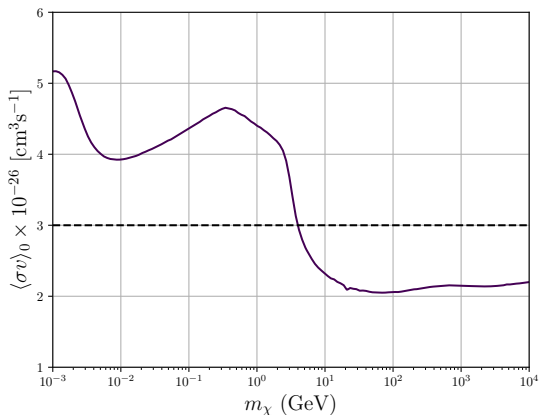
# Motivation

- ① For decades, WIMPs have been the de facto DM candidates
  - ① **Naturally produce DM with correct relic density via freeze-out**

$$\frac{\Omega_\chi h^2}{0.12} \sim \left( \frac{2 \times 10^{-9} \text{GeV}^{-2}}{\langle \sigma v \rangle} \right) \left( \frac{80}{g_\star} \right)^{1/2} \left( \frac{x_f}{23} \right)$$

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  - ③ **Models with NP at EW scale often accommodate EW scale DM candidate (e.g. MSSM)**

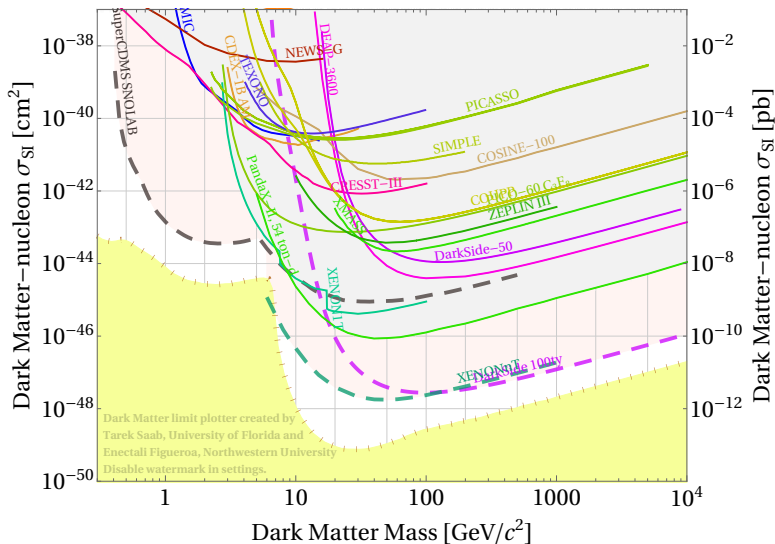
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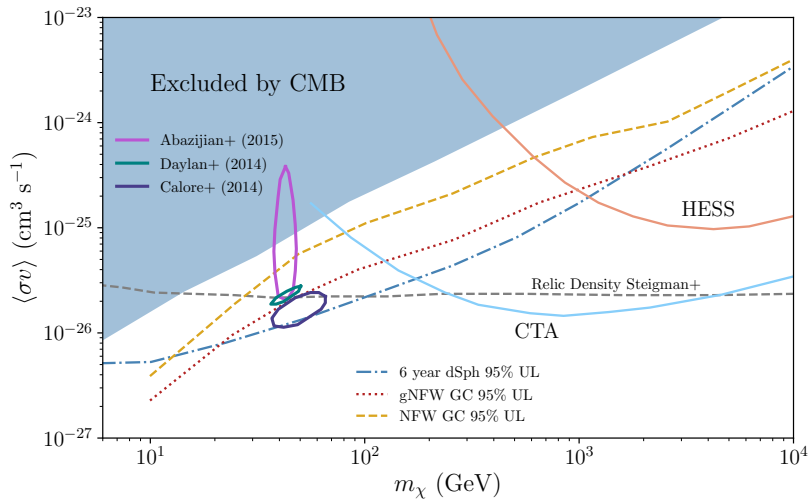
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- ③ **Experiments are putting tight constraints on WIMP models**

# Motivation



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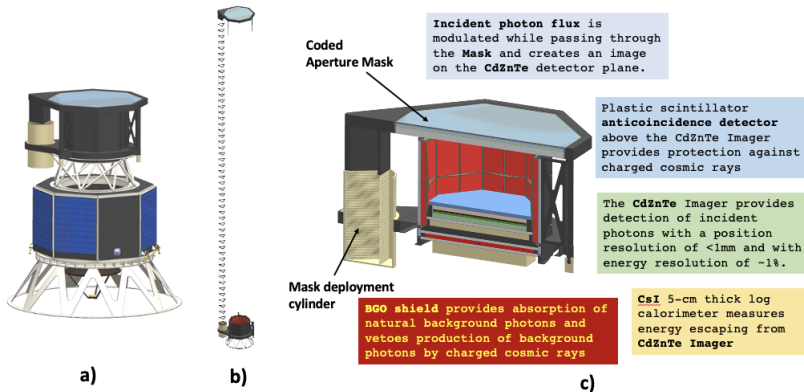


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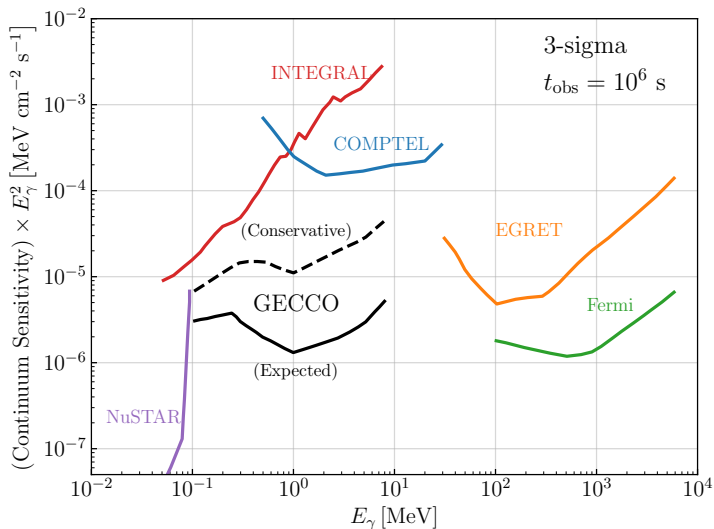
- ① No WIMPs  $\implies$  Explore different mass ranges/mediators
- ② MeV masses much less constrained by current direct and indirect detection experiments
- ③ **Exciting upcoming opportunities to probe MeV DM via indirect detection: AS-Astrogam, AMEGO, GECCO**

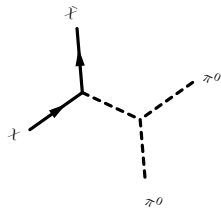
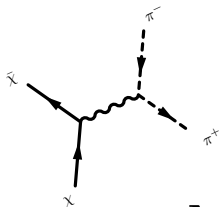


# GECCO

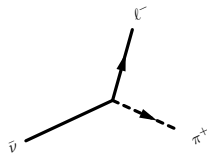


# GECCO Sensitivity





# MeV Dark Matter: From GeV to MeV



A. Coogan, S. Profumo, [LM](#): arXiv:1907.11846

A. Coogan, S. Profumo, [LM](#): arXiv:2104.06168

A. Coogan, A. Moiseev, S. Profumo, [LM](#): arXiv:2101.10370

# Framework

- **Dark Matter models with:**

**Annihilating-DM** :  $0.1 \text{ MeV} \lesssim m_\chi \lesssim 250 \text{ MeV}$

**Decaying-DM** :  $0.1 \text{ MeV} \lesssim m_\chi \lesssim 500 \text{ MeV}$

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(more on this later)

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- **Developed public, open-source python package for comprehensive analysis of MeV DM models**

# HOZMA

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- Facilities to compute constraints from CMB and various PHENO constraints

# Simplified Models

Models:  $\mu \gtrsim \text{GeV}$

- Dark Matter:  $[\text{SU}(3)_c \times \text{SU}(2)_L \times \text{U}(1)_Y]$ -Neutral Dirac Fermion

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$$\mathcal{L}_{\chi(\text{int})} \supset \begin{cases} g_{S\chi} S \bar{\chi} \chi & \text{Scalar Mediator} \\ ig_{P\chi} P \bar{\chi} \gamma^5 \chi & \text{Pseudo-Scalar Mediator} \\ g_{V\chi} V_\mu \bar{\chi} \gamma^\mu \chi & \text{Vector Mediator} \\ g_{A\chi} A_\mu \bar{\chi} \gamma^\mu \gamma^5 \chi & \text{Axial-Vector Mediator} \end{cases}$$

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- Focus on scalar and vector mediator cases
- Also consider RH-neutrino with mixing with a single SM neutrino

$$\begin{pmatrix} \hat{\nu}_k \\ \hat{\bar{\nu}} \end{pmatrix} = \begin{pmatrix} -i \cos \theta & \sin \theta \\ i \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_k \\ \bar{\nu} \end{pmatrix}$$

# Scalar Mediator: $\mu \gtrsim \text{GeV}$

- Add  $\text{SU}(3)_c \otimes \text{SU}(2)_L \otimes \text{U}(1)_Y$  singlet, scalar mediator  $S$  with mass  $m_S$



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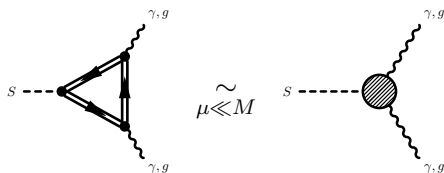
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$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} + \mathcal{L}_\chi - \frac{1}{2}(\partial_\mu S)^2 - V(S) - g_{S\chi} S \bar{\chi} \chi \\ & - S \sum_f g_{Sf} \bar{f} f + \frac{S}{\Lambda} \left( g_{SF} \frac{\alpha_{\text{EM}}}{4\pi} F_{\mu\nu} F^{\mu\nu} + g_{SG} \frac{\alpha_s}{4\pi} G_{\mu\nu}^a G^{\mu\nu,a} \right) \end{aligned}$$

# Higgs Portal: $\mu \gtrsim \text{GeV}$

- Assume the scalar mediator mixes with SM Higgs

$$\begin{pmatrix} \hat{h} \\ \hat{S} \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ S \end{pmatrix}$$

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$$\hat{h} = \cos\theta h - \sin\theta S$$

- Induces interactions between SM and  $S$

$$-\frac{h}{v_h} \sum_{\psi} m_{\psi} \bar{\psi} \psi + \dots \rightarrow -\sin\theta \frac{S}{v_h} \sum_{\psi} m_{\psi} \bar{\psi} \psi + \dots$$

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- Resulting scalar Lagrangian with dimension-5 operators for  $\mu \gtrsim \text{GeV}$

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$$g_{Sf} = \frac{m_f}{v_h} \sin \theta, \quad g_{SF} = \frac{5}{6} \sin \theta, \quad g_{SG} = -3 \sin \theta, \quad \Lambda = v_h$$



## Vector Mediator: $\mu \gtrsim \text{GeV}$

- Add massive U(1) vector  $V_\mu$  via Stueckelberg (or SSB):

$$\begin{aligned} & -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{1}{2}(\partial_\mu\sigma + m_V V_\mu)^2 - \frac{1}{2\xi}(\partial_\mu V^\mu - \xi m\sigma)^2 \\ & \longrightarrow \frac{1}{2}V_\mu \left[ \left( \square + m_V^2 \right) g^{\mu\nu} - \left( 1 - \frac{1}{\xi} \right) \partial^\mu \partial^\nu \right] V_\nu + \dots \end{aligned}$$

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- Vector Lagrangian for  $\mu \gtrsim \text{GeV}$

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- Result

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} + \mathcal{L}_\chi + \frac{1}{2} V_\mu \left[ (\square + m_V^2) g^{\mu\nu} - \partial^\mu \partial^\nu \right] V_\nu \\ & + g_{V\chi} V_\mu \bar{\chi} \gamma^\mu \chi + \sum_f g_{Vf} V_\mu \bar{f} \gamma^\mu f \end{aligned}$$

$$g_{Vf} = -\epsilon e Q_f$$

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Charged Currents:

$$J_{\mu}^{+} = \sum_i \nu_i^{\dagger} \bar{\sigma}_{\mu} \ell_i + \sum_{i,j} V_{ij}^{\text{CKM}} u_i^{\dagger} \bar{\sigma}_{\mu} d_j$$

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Neutral Currents:

$$J_\mu^Z = \frac{1}{c_W} \sum_f g_{f,L}^Z f^\dagger \bar{\sigma}_\mu f + \frac{1}{c_W} \sum_{\bar{f}} g_{f,R}^Z \bar{f}^\dagger \bar{\sigma}_\mu \bar{f}$$

$$g_{f,L}^Z = T_f^3 - Q_f s_W^2$$

$$g_{f,R}^Z = -Q_f s_W^2$$

# Decent to MeV Scale

# Moving below 1 GeV

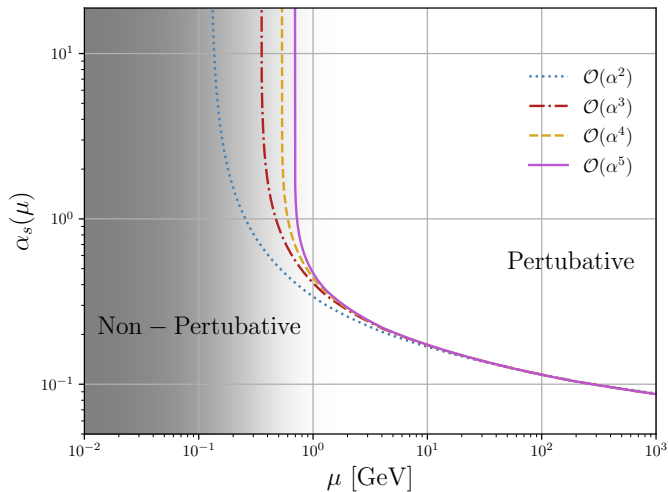
Now that we have the Lagrangians above 1 GeV, we need to determine the Lagrangians below 1 GeV

$$\mathcal{L}_{\mu > 1\text{GeV}}$$



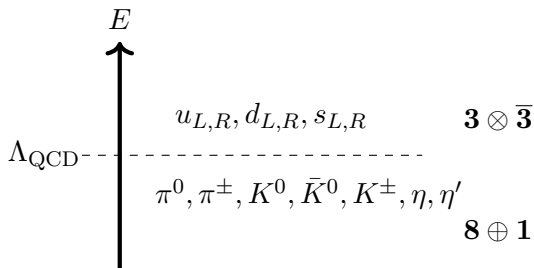
$$\mathcal{L}_{\mu < 1\text{GeV}} \sim \mathcal{L}_{\text{ChiPT}}$$

# Moving below 1 GeV



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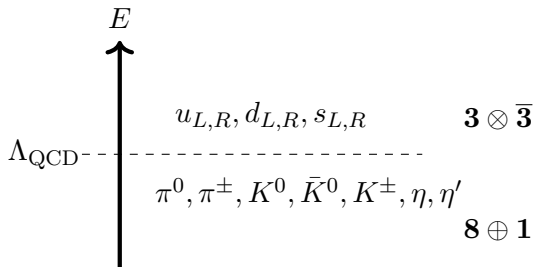
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- Use an effective Lagrangian below 1 GeV : **Chiral Lagrangian**

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- Need low-energy Lagrangian describing pions, etc. to obey the symmetries of  $\mathcal{L}_{\text{QCD}}^{\text{light}}$

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- Symmetric under global  $\text{SU}(3)_L \otimes \text{SU}(3)_R$  symmetry in chiral limit

$$\mathbf{q} \equiv \begin{pmatrix} u \\ d \\ s \end{pmatrix} \rightarrow e^{i\theta_L^a \lambda^a / 2} \begin{pmatrix} u \\ d \\ s \end{pmatrix} \quad \bar{\mathbf{q}} \equiv \begin{pmatrix} \bar{u} \\ \bar{d} \\ \bar{s} \end{pmatrix} \rightarrow e^{i\theta_R^a \lambda^a / 2} \begin{pmatrix} \bar{u} \\ \bar{d} \\ \bar{s} \end{pmatrix}$$

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- CCWZ tells us how to construct bottom-up Lagrangian for pseudo-Goldstones generated from symmetry breaking

# Chiral Lagrangian

The Chiral Lagrangian is

$$\mathcal{L} = \frac{f_\pi^2}{4} \text{Tr}(D_\mu \Sigma^\dagger D^\mu \Sigma) + \frac{f_\pi^2}{4} \text{Tr}(\chi \Sigma^\dagger + \Sigma \chi^\dagger)$$

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where

$$\Sigma = \exp \left( \frac{i\sqrt{2}}{f_\pi} \Pi^a \lambda_a \right), \quad \Sigma \rightarrow U_R \Sigma U_L^\dagger$$

$\Pi^a$  are the NGB

$\lambda_a$  Gell-Mann matrices

$$\sqrt{2} \Pi^a \lambda_a = \begin{pmatrix} \pi^0 + \frac{1}{\sqrt{3}} \eta & \sqrt{2} \pi^+ & \sqrt{2} K^+ \\ \sqrt{2} \pi^- & -\pi^0 + \frac{1}{\sqrt{3}} \eta & \sqrt{2} K^0 \\ \sqrt{2} K^- & \sqrt{2} K^0 & -\frac{2}{\sqrt{3}} \eta \end{pmatrix}$$



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where

$$D_\mu \Sigma = \partial_\mu \Sigma - i \mathbf{r}_\mu \Sigma + i \Sigma \mathbf{l}_\mu$$

and  $\mathbf{l}_\mu$  and  $\mathbf{r}_\mu$  are left- and right-handed currents associated with a local  $\text{SU}(3)_L \otimes \text{SU}(3)_R$  symmetry

$$\mathbf{l}_\mu \rightarrow U_L \mathbf{l}_\mu U_L^\dagger$$

$$\mathbf{r}_\mu \rightarrow U_R \mathbf{r}_\mu U_R^\dagger$$

$$D_\mu \Sigma \rightarrow U_R (D_\mu \Sigma) U_L^\dagger$$

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where

$$\chi = 2B_0(\mathbf{s} + i\mathbf{p}), \quad \chi \rightarrow U_R \chi U_L^\dagger$$

and  $\mathbf{s}, \mathbf{p}$  are the scalar and pseudo-scalar current densities and

$$B_0 = \frac{m_\pi^2}{m_u + m_d} \approx 2600 \text{ MeV}$$

Without any external fields,

$$\mathbf{s} = \text{diag}(m_u, m_d, m_s)$$

# Matching

# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching

- Below  $1\text{GeV}$   $\mathcal{L}_{\text{QCD}} \rightarrow \mathcal{L}_{\chi\text{PT}}$

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- Operators that need to be matched:

$$S\bar{q}\mathbf{G}Sqq, \quad \bar{q}\gamma^\mu(\ell_\mu P_L + \mathbf{r}_\mu P_R)\mathbf{q}, \quad SG_{\mu\nu}^a G^{a,\mu\nu}$$

Matching:  $S\bar{q}G_{S_q}q$

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- Matched onto ChiPT mass term:

$$-\bar{q}(M_q + SG_{Sq})q \rightarrow \frac{f_\pi^2}{4} \text{Tr}[\chi \Sigma^\dagger + \text{c.c.}], \quad \chi = 2B(M_q + SG_{Sq})$$

Matching:  $\bar{\mathbf{q}}\gamma^\mu(\boldsymbol{\ell}_\mu P_L + \mathbf{r}_\mu P_R)\mathbf{q}$

- Current transform as

$$\mathbf{r}_\mu \rightarrow \mathbf{U}_R \mathbf{r}_\mu \mathbf{U}_R^\dagger,$$

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- Matching currents is done using via a connection

$$D_\mu \boldsymbol{\Sigma} = \partial_\mu \boldsymbol{\Sigma} - i\mathbf{r}_\mu \boldsymbol{\Sigma} + i\boldsymbol{\Sigma} \boldsymbol{\ell}_\mu$$

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$$\bar{\mathbf{q}}\gamma^\mu(V_\mu \mathbf{G}_{Vq})\mathbf{q} \rightarrow \frac{f_\pi^2}{4} \text{Tr}[(D_\mu \boldsymbol{\Sigma})^\dagger (D_\mu \boldsymbol{\Sigma})]$$
$$\boldsymbol{\ell}_\mu = \mathbf{r}_\mu = V_\mu \mathbf{G}_{Vq} = V_\mu \text{diag}(g_{Vu}, g_{Vd}, g_{Vs})$$

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- Additional term from chiral anomaly (Wess-Zumino-Witten):

$$-\frac{e^2}{32\pi^2} F_{\mu\nu} \tilde{F}^{\mu\nu} \frac{\pi^0}{f_\pi} \rightarrow -\frac{e^2}{32\pi^2} F_{\mu\nu} \tilde{F}^{\mu\nu} \frac{\pi^0}{f_\pi} - \frac{\epsilon e^2}{16\pi^2} F_{\mu\nu} \tilde{V}^{\mu\nu} \frac{\pi^0}{f_\pi}$$

Matching:  $SG_{\mu\nu}^a G^{\mu\nu,a}$

- Use trace anomaly and RG invariance of scale divergence:

$$\partial_\mu d^\mu = \theta_\mu^\mu$$



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- Scale divergence for  $\mu > \text{GeV}$

$$\partial_\mu d^\mu \sim \frac{\beta}{2g_s} G^2 + \sum_q (1 - \gamma_m) m_q \bar{q}q + \dots$$

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- Scalar interaction is:

$$g_{SG} \frac{\alpha}{4\pi} \frac{S}{\Lambda} G^2 \rightarrow -\frac{2g_{SG}}{\beta_0} \frac{S}{\Lambda} \partial_\mu d^\mu + \frac{2g_{SG}}{\beta_0} \frac{S}{\Lambda} \sum_q m_q \bar{q}q + \dots$$

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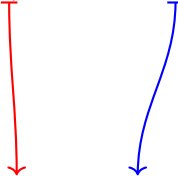
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- Matched onto ChiPT Lagrangian by computing  $\partial_\mu d^\mu$

$$\partial_\mu d^\mu = -\frac{f_\pi^2}{2} \text{Tr} \left[ (D_\mu \Sigma)^\dagger (D_\mu \Sigma) \right] - f_\pi^2 \text{Tr} \left[ \chi \Sigma^\dagger + \text{c.c.} \right]$$

# Matching: Dictionary

$$\mathcal{L}_{\mu > \text{GeV}} \supset \bar{\mathbf{q}} \mathbf{r}_\mu \gamma^\mu P_R \mathbf{q} + \bar{\mathbf{q}} \mathbf{l}_\mu \gamma^\mu P_L \mathbf{q} + \bar{\mathbf{q}} \mathbf{s} \mathbf{q} + \phi \frac{\alpha}{4\pi} G_{\mu\nu}^a G^{\mu\nu, a}$$



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$$\chi = 2B_0 \left( s + \left( 1 - \frac{2}{\beta_0} \phi \right) M_q \right)$$

$$\begin{aligned} \mathcal{L}_{\mu < \text{GeV}} \supset & \frac{f_\pi^2}{4} \text{Tr} \left[ (D_\mu \Sigma)^\dagger (D_\mu \Sigma) \right] + \frac{f_\pi^2}{4} \text{Tr} \left[ \chi \Sigma^\dagger + \text{c.c.} \right] \\ & - \frac{f_\pi^2}{\beta_0} \phi \text{Tr} \left[ (D_\mu \Sigma)^\dagger (D_\mu \Sigma) \right] + \frac{2f_\pi^2}{\beta_0} \phi \text{Tr} \left[ \chi \Sigma^\dagger + \text{c.c.} \right] \end{aligned}$$

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$$\underbrace{D_\mu \boldsymbol{\Sigma} = \partial_\mu \boldsymbol{\Sigma} - i \mathbf{r}_\mu \boldsymbol{\Sigma} + i \boldsymbol{\Sigma} \boldsymbol{\ell}_\mu}_{\text{Left side of } \mathcal{L}_{\mu < \text{GeV}}}$$

$$\underbrace{\boldsymbol{\chi} = 2B_0 \left( \mathbf{s} + \left( 1 - \frac{2}{\beta_0} \phi \right) M_q \right)}_{\text{Right side of } \mathcal{L}_{\mu < \text{GeV}}}$$

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# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching - **vector**

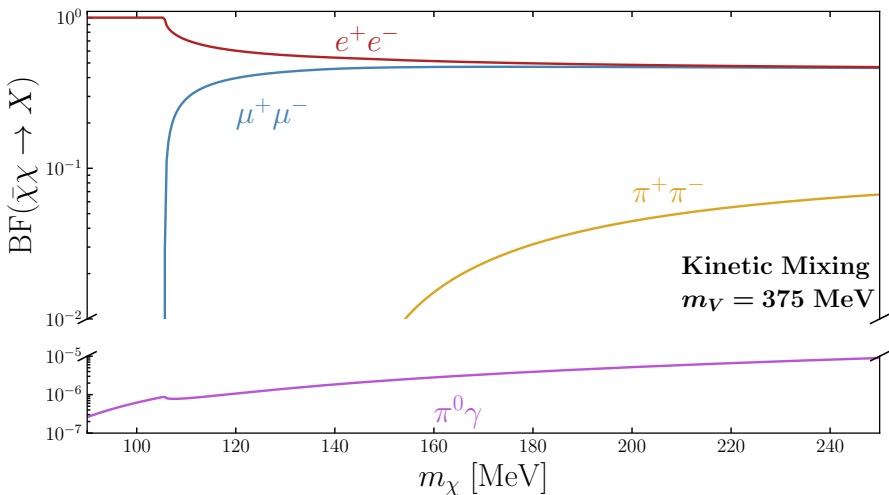
- Below a GeV

$$\begin{aligned}\mathcal{L}_V \supset & g_{V\chi} V_\mu \bar{\chi} \gamma^\mu \chi + \sum_\ell g_{V\ell} V_\mu \bar{\ell} \gamma^\mu \ell \\ & + \frac{f_\pi^2}{4} \text{Tr} \left( (D_\mu \Sigma)^\dagger D_\mu \Sigma \right) + \frac{f_\pi^2}{4} \text{Tr} \left( \chi \Sigma^\dagger + \Sigma \chi^\dagger \right)\end{aligned}$$

with

$$\begin{aligned}D_\mu \Sigma &= \partial_\mu \Sigma - i r_\mu \Sigma + i \Sigma \ell_\mu \\ \chi &= 2B_0 s \\ s &= \text{diag}(m_u, m_d, m_s) \\ r_\mu = \ell_\mu &= -e A_\mu \text{diag} \left( \frac{2}{3}, -\frac{1}{3}, -\frac{1}{3} \right) + V_\mu \text{diag}(g_{Vu}, g_{Vd}, g_{Vs})\end{aligned}$$

# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching - vector



## From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching- **scalar**

- Below 1 GeV, we have

$$\begin{aligned}\mathcal{L}_S \supset & g_{S\chi} S \bar{\chi} \chi + g_{fV} \frac{S}{v} \sum_{\ell} m_{\ell} \bar{\ell} \ell + \frac{\alpha_{\text{EM}}}{4\pi\Lambda} g_{SF} S F^2 \\ & + \frac{f_{\pi}^2}{4} \text{Tr} \left( (D_{\mu} \Sigma)^{\dagger} D_{\mu} \Sigma \right) + \frac{f_{\pi}^2}{4} \text{Tr} \left( \chi \Sigma^{\dagger} + \Sigma \chi^{\dagger} \right) \\ & + \frac{2g_G}{9v} S \left( \frac{f_{\pi}^2}{2} \text{Tr} \left( (D_{\mu} \Sigma)^{\dagger} (D^{\mu} \Sigma) \right) + f_{\pi}^2 \text{Tr} \left( \chi \Sigma^{\dagger} + \Sigma \chi^{\dagger} \right) \right)\end{aligned}$$

with

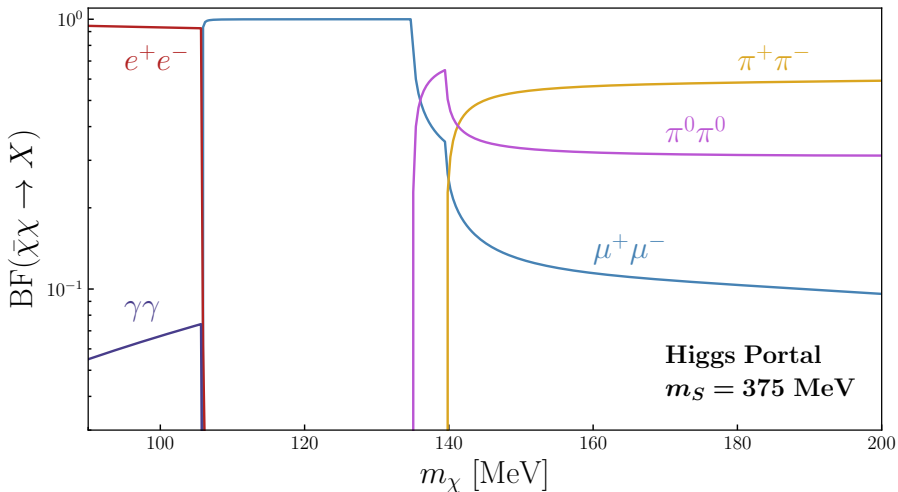
$$D_{\mu} \Sigma = \partial_{\mu} \Sigma - i r_{\mu} \Sigma + i \Sigma \ell_{\mu}$$

$$\chi = 2B_0 s$$

$$s = \text{diag}(m_u, m_d, m_s) \left( 1 + g_S f \frac{S}{v} \right)$$

$$r_{\mu} = \ell_{\mu} = -e A_{\mu} \text{diag} \left( \frac{2}{3}, -\frac{1}{3}, -\frac{1}{3} \right)$$

# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching- scalar



# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching- **RHN**

$$\mathcal{L}_{\bar{\nu}(\text{int})} = \frac{f_\pi^2}{4} \text{Tr} \left[ |\partial_\mu \Sigma - i \mathbf{r}_\mu \Sigma + i \Sigma \boldsymbol{\ell}_\mu|^2 \right]$$

Currents:

$$\mathbf{r}_\mu = -\frac{8G_F}{\sqrt{2}} \mathbf{G}_R R_\mu^0, \quad \boldsymbol{\ell}_\mu = -\frac{4G_F}{\sqrt{2}} \left( 2\mathbf{G}_L L_\mu^0 + \mathbf{V}^\dagger L_\mu^- \right)$$

$$L_\mu^0 = \frac{\sin(2\theta)}{4c_W} \delta_{ik} \left( \nu_i^\dagger \bar{\sigma}_\mu \bar{\nu} + \text{c.c.} \right) + \frac{1}{2c_W} \left( -1 + 2s_W^2 \right) \ell_i^\dagger \bar{\sigma}_\mu \ell_i$$

$$L_\mu^- = \sin \theta \delta_{ik} \ell_i^\dagger \bar{\sigma}_\mu \bar{\nu}$$

$$R_\mu^0 = \frac{s_W^2}{c_W} \bar{\ell}_i^\dagger \bar{\sigma}_\mu \bar{\ell}_i$$

# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching- **RHN**

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Currents:

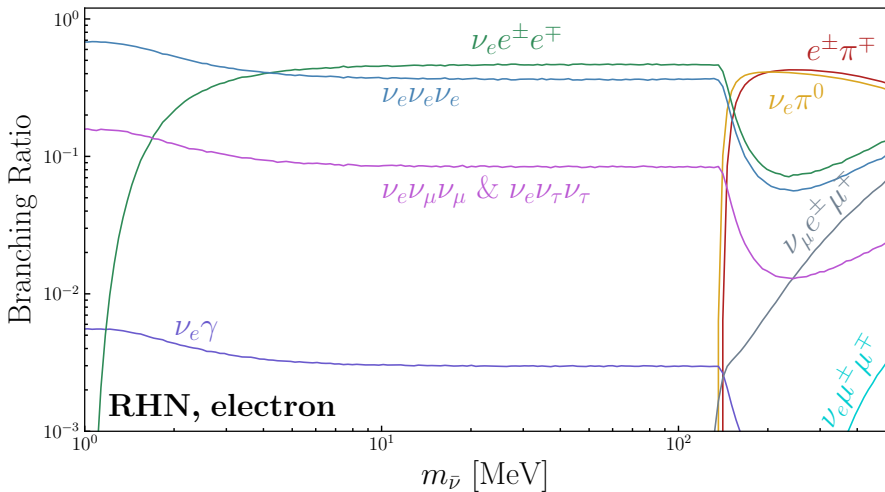
$$\mathbf{r}_\mu = 2\mathbf{G}_R R_\mu^0, \quad \boldsymbol{\ell}_\mu = 2\mathbf{G}_L L_\mu^0 + \mathbf{V}^\dagger L_\mu^-$$

$$\mathbf{G}_R = -\frac{s_W^2}{3c_W} \text{diag}(2, -1, -1)$$

$$\mathbf{G}_L = \frac{1}{2c_W} \text{diag}(1, -1, -1) + \mathbf{G}_R$$

$$\mathbf{V} = \begin{pmatrix} 0 & V_{ud} & V_{us} \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

# From $\mu > 1\text{GeV}$ to $\mu < 1\text{GeV}$ : Matching- **RHN**





# Validity of ChiPT

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- Chiral perturbation theory has a limited range of validity
- The chiral expansion is

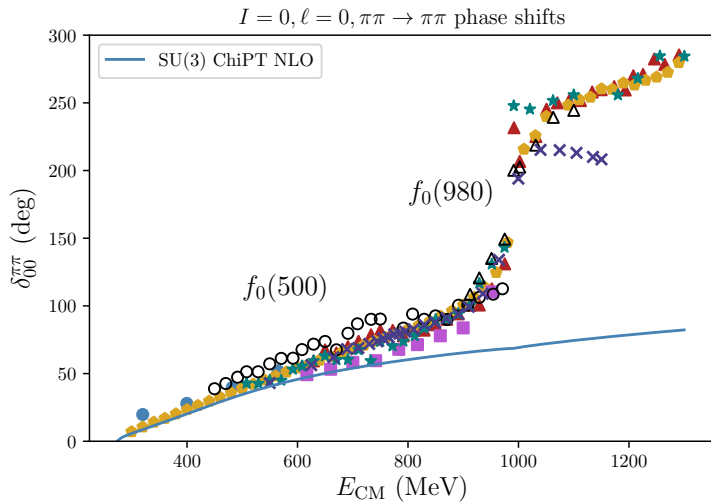
$$\mathcal{L} = \mathcal{L}_2 + \mathcal{L}_4 + \dots$$

$$\mathcal{M} \sim \left(\frac{p^2}{\Lambda_\chi^2}\right) \mathcal{M}^{(2)} + \left(\frac{p^2}{\Lambda_\chi^2}\right)^2 \mathcal{M}^{(4)} + \dots$$

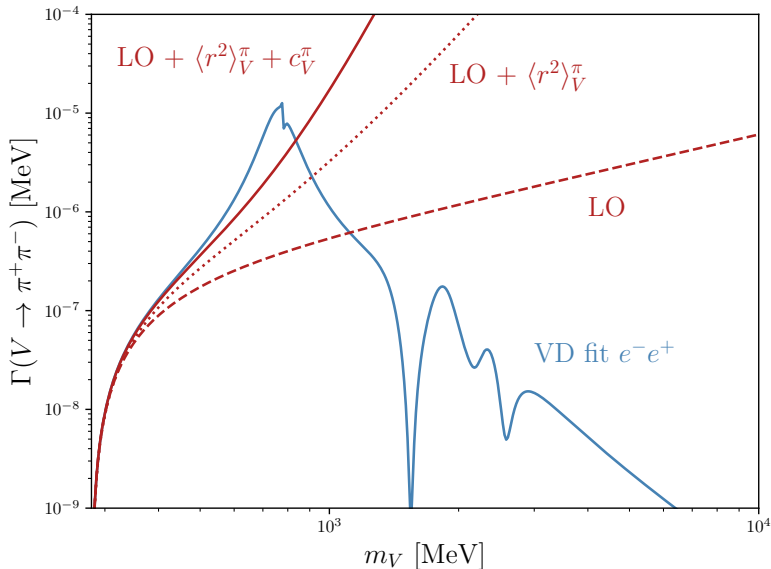
$$\underbrace{\text{Diagram 1}}_{\mathcal{O}(p^2/\Lambda_\chi^2)} + \underbrace{\text{Diagram 2} + \text{Diagram 3}}_{\mathcal{O}(p^4/\Lambda_\chi^4)} + \dots$$

where  $\Lambda_\chi \approx 4\pi f_\pi \approx 1.2 \text{ GeV}$

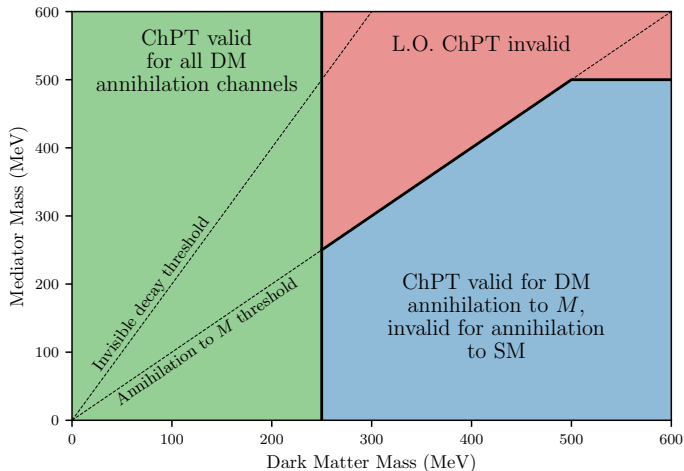
# Validity of ChiPT



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# Validity of ChiPT





# Indirect Detection

- Gamma ray flux observed by detector

$$\frac{d\Phi}{dE_\gamma} = \frac{\Delta\Omega}{4\pi m_\chi^a} \cdot \left[ \frac{1}{\Delta\Omega} \int d\Omega \int_{\text{LOS}} d\ell \rho_\chi^a \right] \cdot \Gamma \cdot \frac{dN}{dE_\gamma}$$



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Integral along detector's “Line-of-sight” of dark matter density of target with angular size  $\Delta\Omega$

$a = 2$  for annihilating DM

$a = 1$  for decaying DM

Target	[MeV <sup>2</sup> cm <sup>-5</sup> sr <sup>-1</sup> ]		[MeVcm <sup>-2</sup> sr <sup>-1</sup> ]	
	$J(1')$	$J(5^\circ)$	$D(1')$	$D(5^\circ)$
Galactic Center (NFW)	$6.972 \times 10^{32}$	$1.782 \times 10^{30}$	$4.84 \times 10^{26}$	$1.597 \times 10^{26}$
Galactic Center (Einasto)	$5.987 \times 10^{34}$	$4.965 \times 10^{31}$	$4.179 \times 10^{27}$	$2.058 \times 10^{26}$
Draco (NFW)	$3.418 \times 10^{30}$	$8.058 \times 10^{26}$	$5.949 \times 10^{25}$	$1.986 \times 10^{24}$
M31 (NFW)	$1.496 \times 10^{31}$	$1.479 \times 10^{27}$	$3.297 \times 10^{26}$	$4.017 \times 10^{24}$

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DM interaction rate:

$$\text{Annihilating DM : } \Gamma = \frac{\langle\sigma v\rangle}{2f_\chi}$$

$$\text{Decaying DM : } \Gamma = \frac{1}{\tau}$$

# Indirect Detection

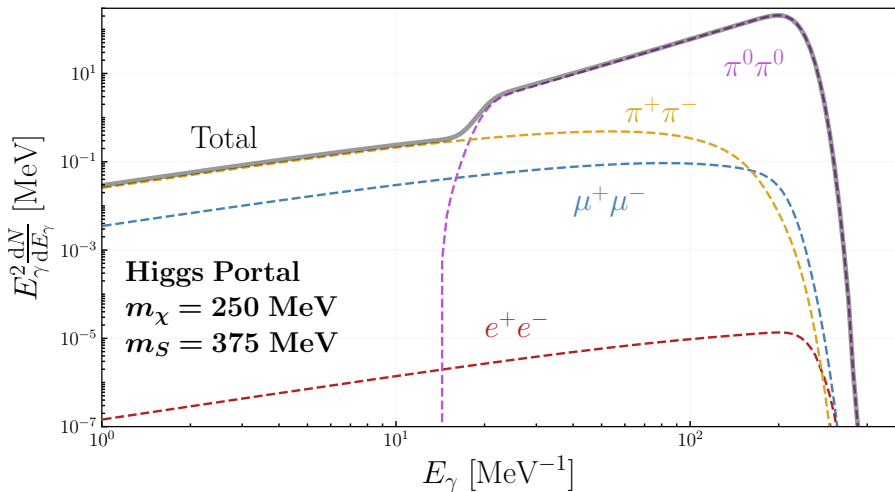
- Gamma ray flux observed by detector

$$\frac{d\Phi}{dE_\gamma} = \frac{\Delta\Omega}{4\pi m_\chi^a} \cdot \left[ \frac{1}{\Delta\Omega} \int d\Omega \int_{\text{LOS}} d\ell \rho_\chi^a \right] \cdot \Gamma \cdot \frac{dN}{dE_\gamma}$$

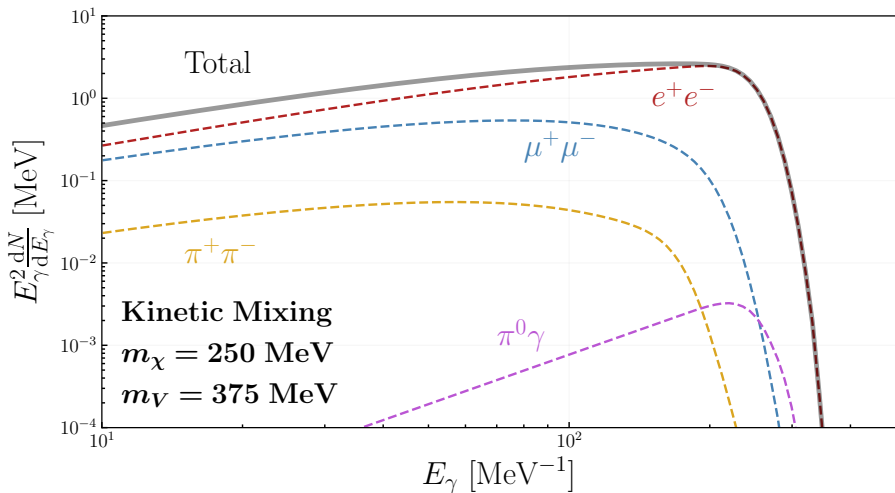
Photon spectrum per annihilation/decay:

$$\frac{dN}{dE_\gamma} = \sum_X \text{BR}(\bar{\chi}\chi \rightarrow \gamma + X) \frac{dN_{\bar{\chi}\chi \rightarrow \gamma + X}}{dE_\gamma}$$

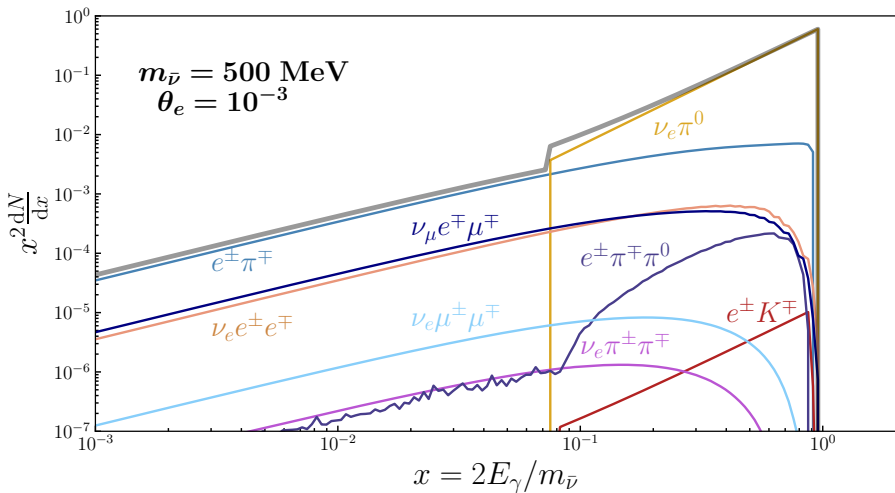
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- Including detector energy resolution

$$\frac{d\bar{\Phi}}{dE_\gamma} = \int d\tilde{E}_\gamma R_\epsilon(E_\gamma|\tilde{E}_\gamma) \frac{d\bar{\Phi}}{d\tilde{E}_\gamma}$$

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Detector energy resolution  $\sim$  Gaussian:

$$R_\epsilon(E_\gamma|\tilde{E}_\gamma) \sim \frac{1}{\sqrt{2\pi}} \frac{1}{\epsilon\tilde{E}} \exp\left(-\frac{1}{2} \left(\frac{\tilde{E} - E}{\epsilon\tilde{E}}\right)^2\right)$$



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- Observed photon count in energy bin  $(E_{\min}^{(i)}, E_{\max}^{(i)})$

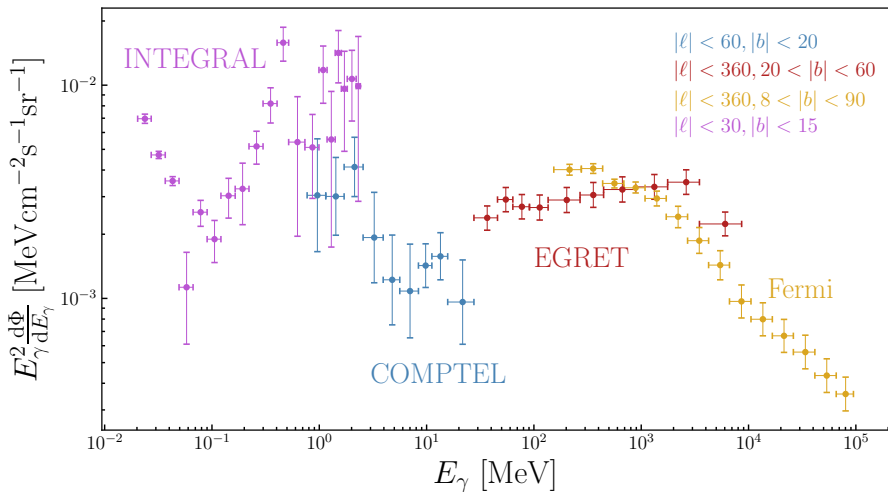
$$N_\gamma = \int_{E_{\min}^{(i)}}^{E_{\max}^{(i)}} dE_\gamma T_{\text{obs}} A_{\text{eff}}(E_\gamma) \frac{d\bar{\Phi}}{dE_\gamma}$$

# Constraining

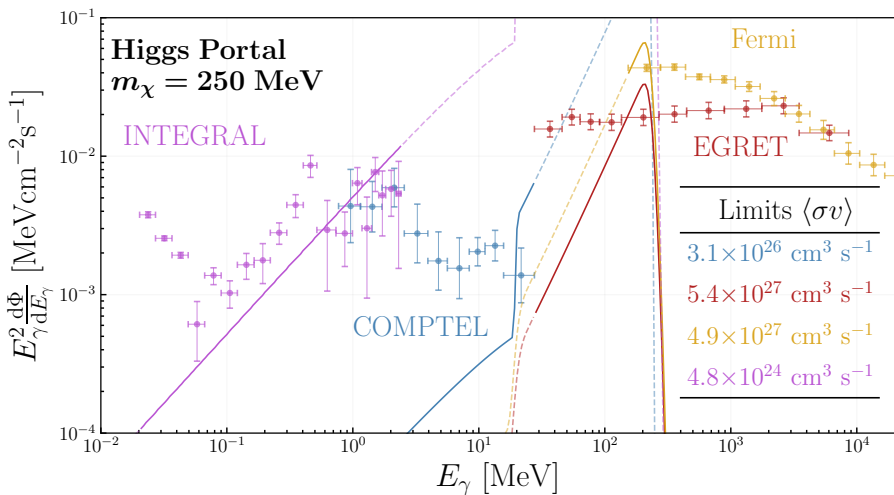
- For telescopes with reported data, constrain by asserting DM signal no greater than twice the upper error

$$\left[ \int_{E_{\text{low}}^{(i)}}^{E_{\text{high}}^{(i)}} dE_{\gamma} \frac{d\Phi_{\gamma}}{dE_{\gamma}} \right] \leq \Phi_{\gamma}^{(i)} + 2\delta\Phi_{\gamma}^{(i)}, \quad i \in 1, \dots, N_{\text{bins}}$$

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- For projecting constraints we maximize the SNR w.r.t. upper and low energy range and restrict the result to be less than  $5\sigma$

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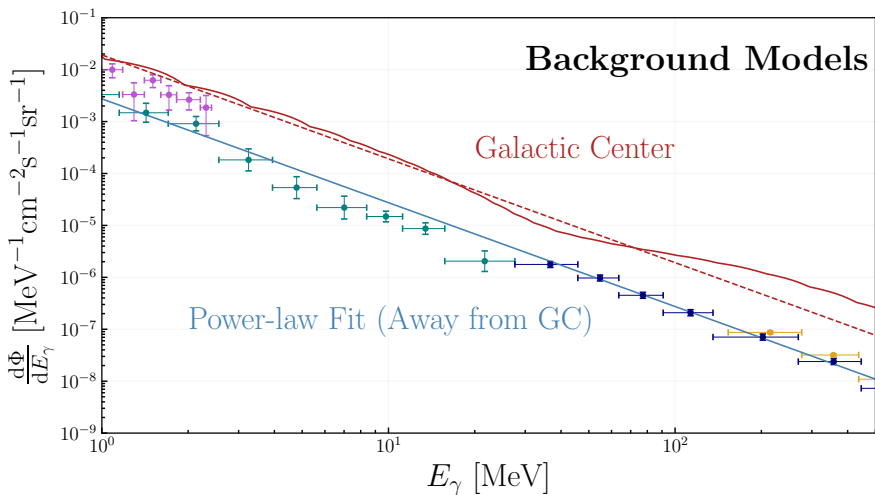
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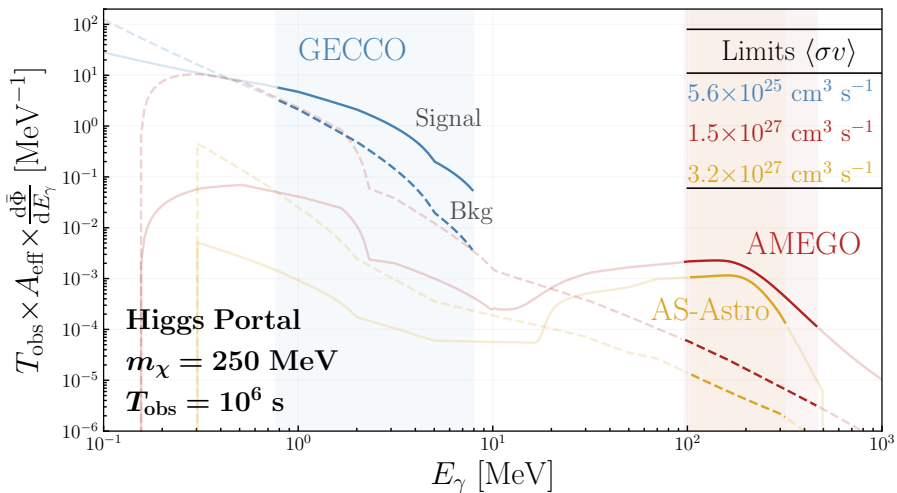
- Use more sophisticated model for Galactic center with bremsstrahlung,  $\pi^0$  and inverse-Compton computed with GALPROP



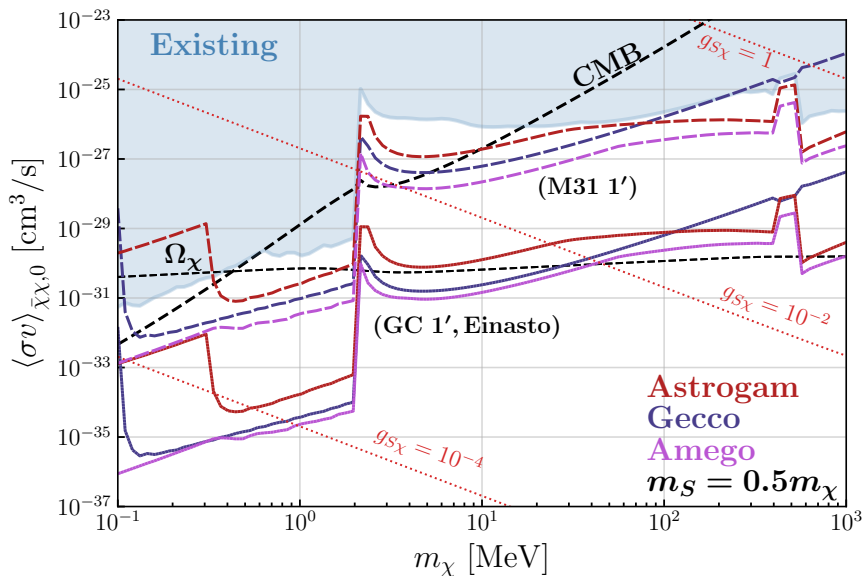
# Constraining



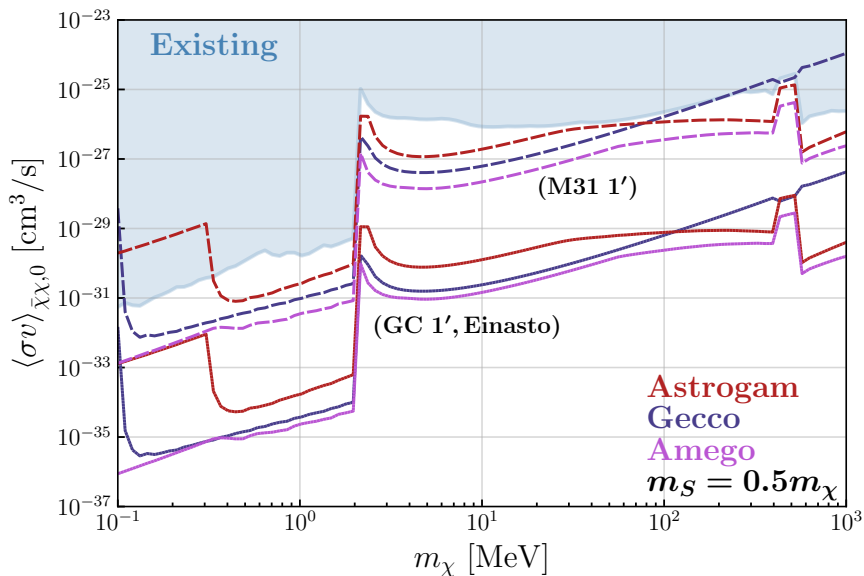
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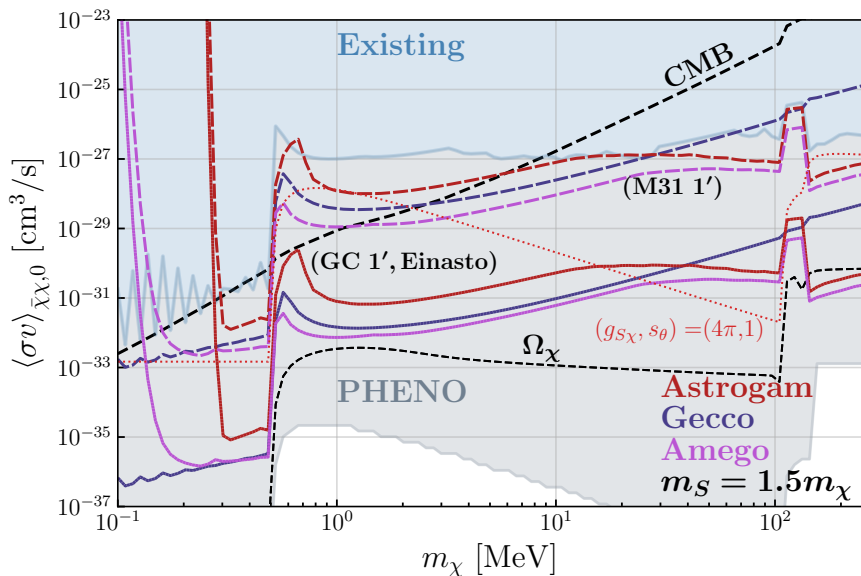
# Higgs Portal Constraints



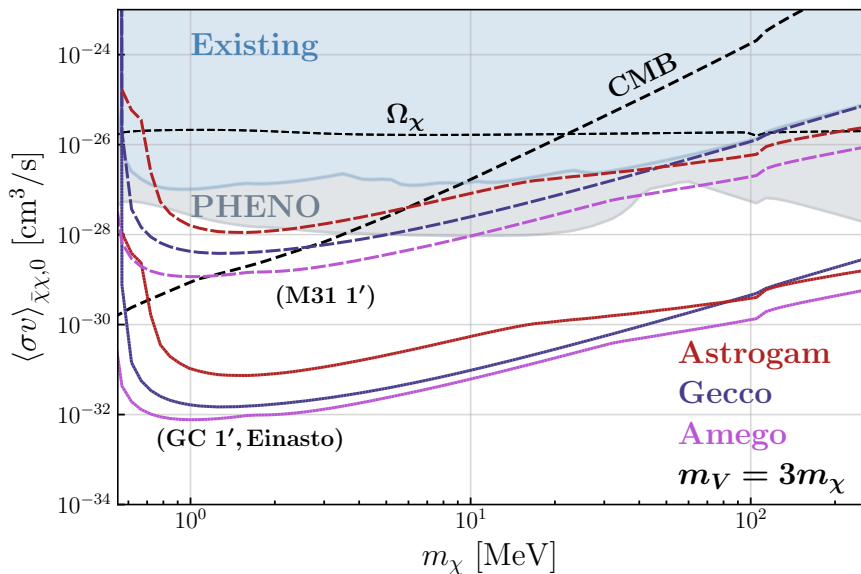
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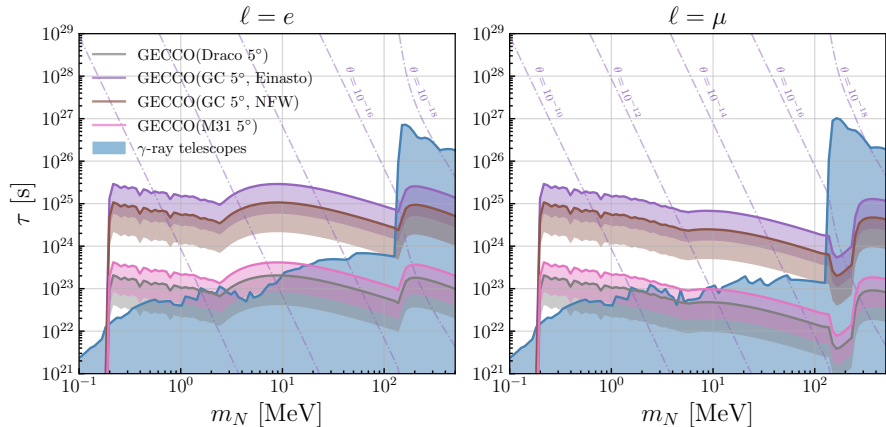
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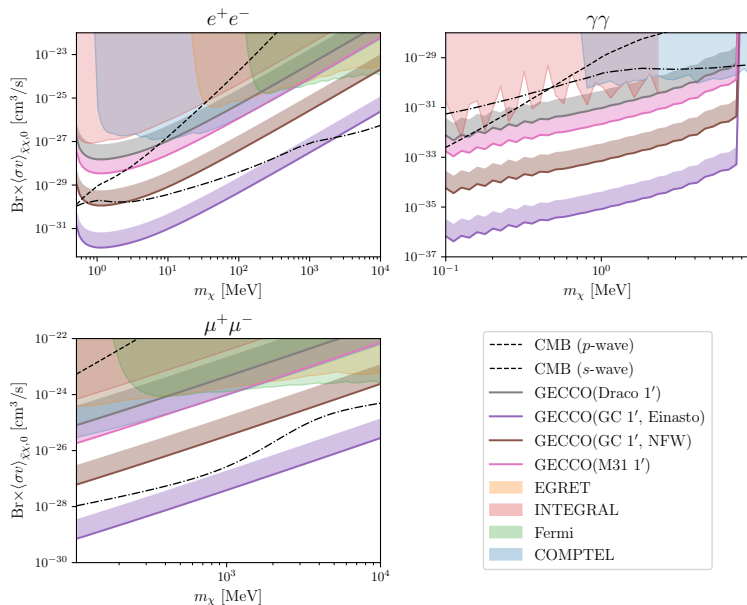
# Kinetic Mixing Constraints



# RH Neutrino Constraints

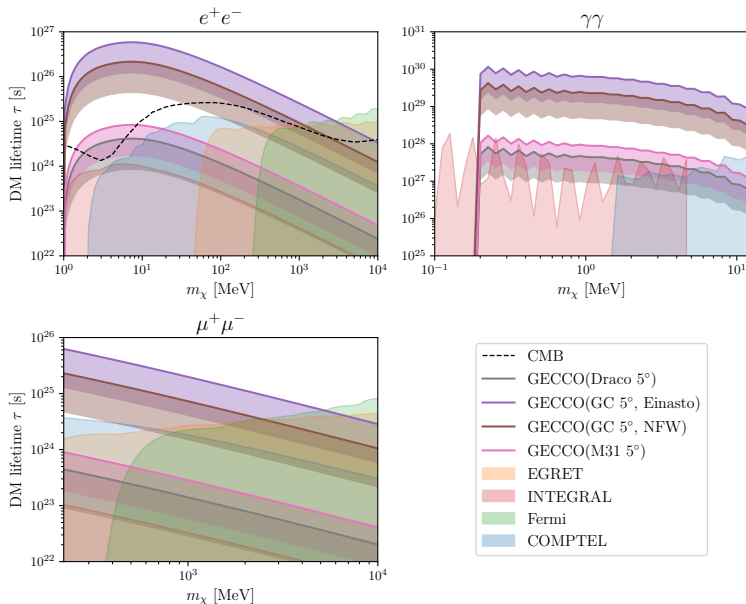


# Model Independent Constraints





# Model Independent Constraints



# Primordial Black Holes

A. Coogan, S. Profumo, **LM**: arXiv:2010.04797

A. Coogan, S. Profumo, **LM**: arXiv:2101.10370

# Hawking Radiation

- ① Can MeV telescopes be used to probe Hawking radiation for PBH?

# Hawking Radiation

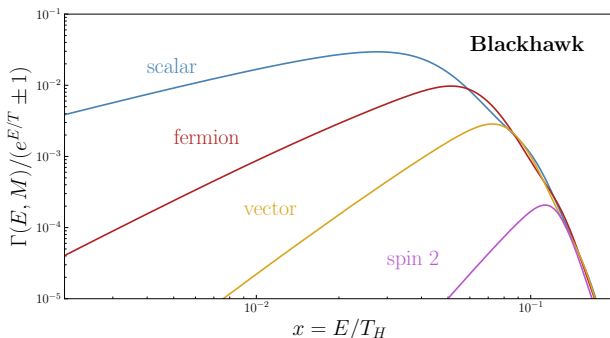
- ① Can MeV telescopes be used to probe Hawking radiation for PBH?
- ② Primary emission rates

$$\frac{\partial^2 N}{\partial E_i \partial t} = \frac{1}{2\pi} \frac{\Gamma(E_i, M)}{e^{E_i/T_H} - (-1)^{2s}}, \quad T_H = \frac{M_{\text{pl}}^2}{8\pi M_H}$$

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- ③ Total photon spectrum

$$\begin{aligned} \frac{\partial^2 N}{\partial E_\gamma \partial t} &= \frac{\partial^2 N_{\gamma, \text{primary}}}{\partial E_\gamma \partial t} + \sum_{i=e^\pm, \mu^\pm, \pi^\pm} \int dE_i \frac{\partial^2 N_{i, \text{primary}}}{\partial E_i \partial t} \frac{dN_\gamma^{\text{FSR}}}{dE_\gamma} \\ &+ \sum_{i=\mu^\pm, \pi^0, \pi^\pm} \int dE_i \frac{\partial^2 N_{i, \text{primary}}}{\partial E_i \partial t} \frac{dN_\gamma^{\text{decay}}}{dE_\gamma} \end{aligned}$$

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Primary spectra:

$$\frac{\partial^2 N_{\gamma, \text{primary}}}{\partial E_\gamma \partial t} = \frac{1}{2\pi} \frac{\Gamma(E_\gamma, M)}{e^{E_\gamma/T_H} - 1}$$



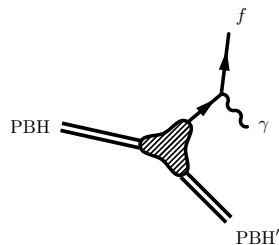
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FSR: ( $x = E_\gamma/E_i$ )

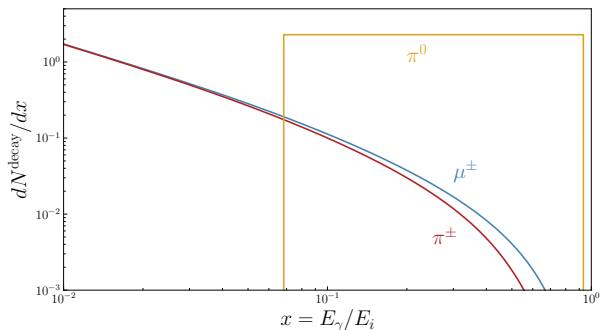
$$\frac{\partial N_\gamma^{\text{FSR}}}{\partial E_\gamma} = \frac{\alpha_{\text{EM}}}{2\pi E_i} P_{\gamma \leftarrow i}(x) \left[ \log\left(\frac{1-x}{\mu_i^2}\right) - 1 \right]$$

$$P_{\gamma \leftarrow i} = \begin{cases} \frac{2(1-x)}{x}, & i = \pi^\pm, \\ \frac{1+(1-x)^2}{x}, & i = e^\pm, \mu^\pm, \end{cases}$$

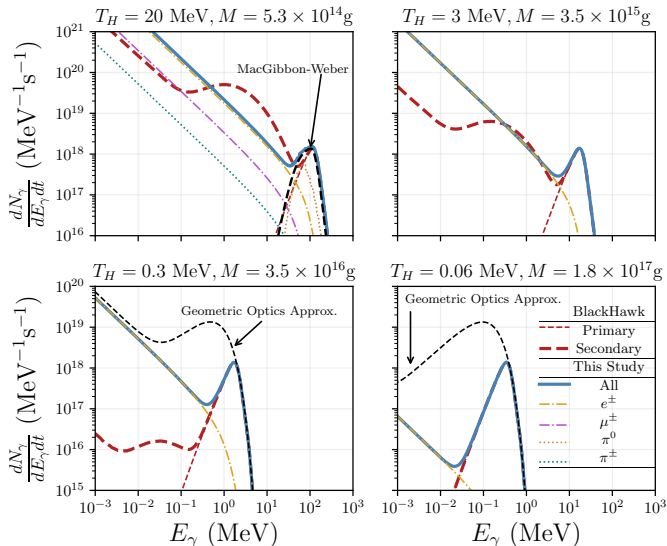


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# Hawking Radiation: Photon Spectrum



# Constraining $f_{\text{PBH}}$

- Given a fraction of DM in the form of (monochromatic) PBHs  $f_{\text{PBH}} = \Omega_{\text{PBH}}/\Omega_{\text{CDM}}$  observed gamma-ray spectrum is:

$$\frac{d\Phi_\gamma}{dE_\gamma} = \frac{1}{4\pi} \int_{\text{LOS}} d\ell \frac{\partial^2 N_\gamma}{\partial E_\gamma \partial t} f_{\text{PBH}} \frac{\rho_{\text{DM}}}{M}$$

# Constraining $f_{\text{PBH}}$

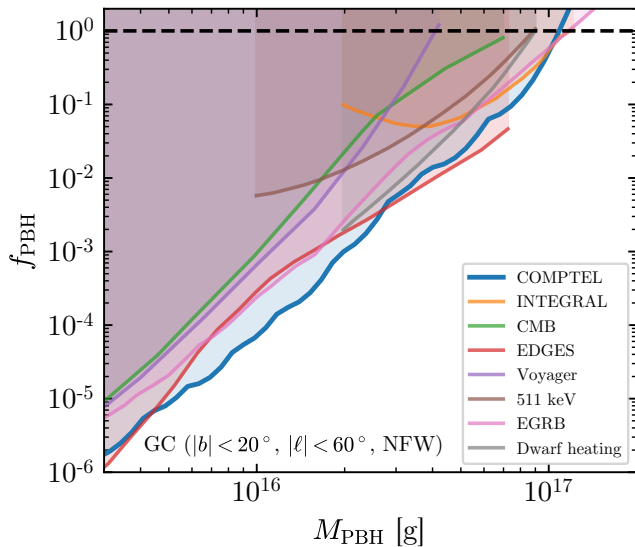
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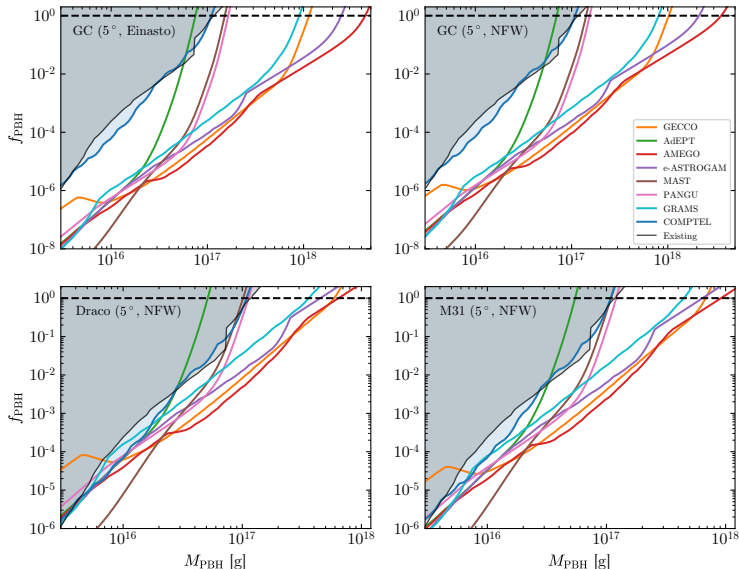
- As with decaying DM, number of observed photons:

$$N_\gamma = T_{\text{obs}} \int_{E_{\text{min}}}^{E_{\text{max}}} dE_\gamma A_{\text{eff}} \int d\tilde{E}_\gamma R_\epsilon(E_\gamma, \tilde{E}_\gamma) \frac{d\Phi}{dE_\gamma}$$

# Constraining $f_{\text{PBH}}$



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# Future Work



# Extending HAZMA to GeV

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- We can exploit  $e^+e^-$  collision data to extract vector form factors using vector meson dominance

$$\mathcal{M} \sim \langle \text{had} | J_{\text{EM}}^\mu | 0 \rangle \langle 0 | \gamma^\mu | \bar{\chi} \chi \rangle$$
$$\langle \text{had} | J_{\text{EM}}^\mu | 0 \rangle = \sum_{T,i} T^\mu \frac{\mathcal{A}_i e^{i\phi_i}}{m_i^2 - s + i\sqrt{s}\Gamma_i(s)}$$

# Extending Hazma to GeV

- Currently we are limited to  $m_\chi \lesssim 250$  MeV ( $\lesssim 500$  MeV for decaying DM)
- Idea: assume DM couplings to quarks via

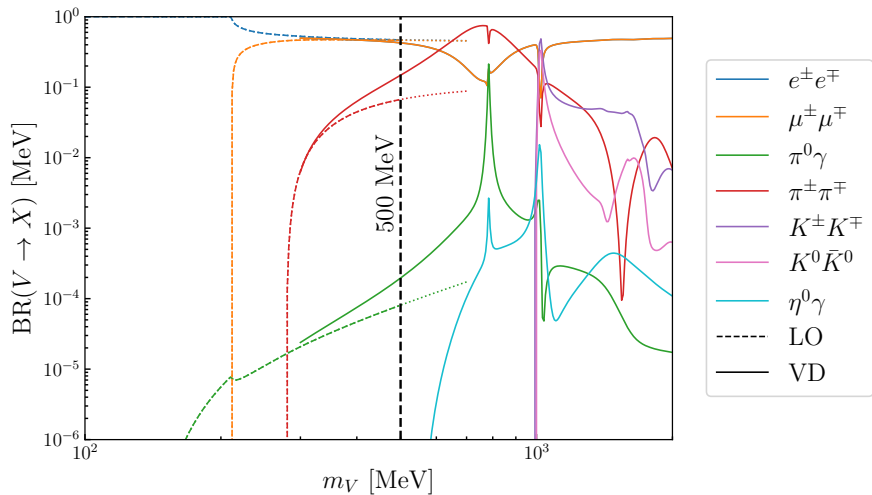
$$\mathcal{L} \supset \sum_q g_{Vq} V_\mu \bar{q} \gamma^\mu q$$

- We can exploit  $e^+e^-$  collision data to extract vector form factors using vector meson dominance

$$\mathcal{M} \sim \langle \text{had} | J_{\text{EM}}^\mu | 0 \rangle \langle 0 | \gamma^\mu | \bar{\chi} \chi \rangle$$
$$\langle \text{had} | J_{\text{EM}}^\mu | 0 \rangle = \sum_{T,i} T^\mu \frac{\mathcal{A}_i e^{i\phi_i}}{m_i^2 - s + i\sqrt{s}\Gamma_i(s)}$$

- How much does this change?

# Extending Hazma to GeV



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# Conclusions

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- **Hazma**: New open-source, user-friendly python package to explore/constrain MeV DM models
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- MeV telescopes could also detect Hawking radiation for  $M_{\text{PBH}} \sim 10^{15} - 10^{18} \text{ g}$

# Thanks

Thanks to everyone who has helped and encouraged me throughout Graduate School...



Happy Holidays!



# Honorable Mentions

Large-Nightmare  
One-Loop Charge Breaking 2HDM  
Asymptotic Analysis of Boltzmann Equation



# Large-*N* Nightmare Dark Matter

Stefano Profumo, Dean J. Robinson, **LM**:  
arXiv:2010.03586

# Theory

- Consider an  $SU(N)$  gauge theory with a single dark (effectively massless,  $m_{\tilde{q}} \ll \Lambda$ ) “quark”
- We take  $N \gg 1$  and assume  $g_{\text{dark}} \sim 1/\sqrt{N}$  (large- $N$  limit)
- Two stable states:  $\tilde{\eta}'$  ( $\bar{q}q$ ) and  $\tilde{\Delta}$  ( $N\tilde{q}$ )
- The  $\tilde{\eta}'$  is very light while the  $\tilde{\Delta}$  very heavy

State	Mass	Lifetime	$U(1)_V$
$\tilde{\eta}'$	$\sim \Lambda/\sqrt{N}$	stable	0
$\tilde{\Delta}$	$\sim N\Lambda$	stable	$N$
$\tilde{\omega}$	$\sim \Lambda$	$N^2/\Lambda$	0
$\tilde{G}$	$\sim \text{few } \Lambda$	$N^2/\Lambda$	0

# Interactions

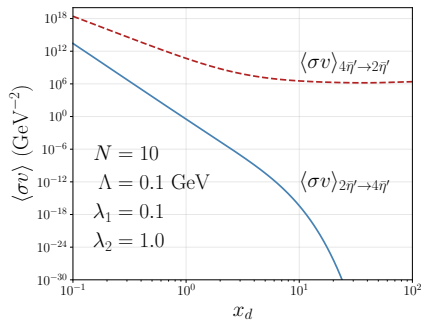
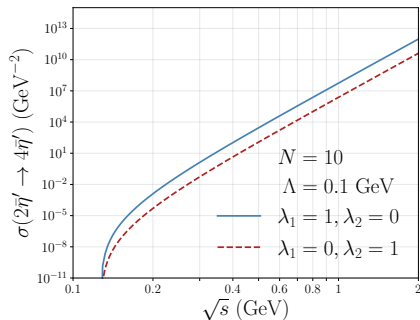
- Interactions for the  $\tilde{\eta}$  are roughly:

$$\sigma_{2\tilde{\eta} \rightarrow 2\tilde{\eta}}(s) \sim \frac{\pi^3 s^3 |\lambda_1|^2}{4\Lambda^8 N^2}, \quad \sigma_{2\tilde{\eta} \rightarrow 4\tilde{\eta}}(s) \sim \frac{\pi^3 s^7}{48\Lambda^{16} N^4} \left| 10\lambda_1^2 + \lambda_2 \right|^2$$

- Interactions for the  $\tilde{\Delta}$  :

$$\sigma_{\tilde{\eta}\tilde{\eta} \rightarrow \tilde{\Delta}\tilde{\Delta}}(s) \sim \frac{e^{-2cN}}{64\pi N^2 \Lambda^2}, \quad \sigma_{\tilde{\Delta}\tilde{\Delta} \rightarrow \tilde{\Delta}\tilde{\Delta}}(s) \sim \frac{4\pi^3}{\Lambda^2}$$

# Interactions



# Thermal Evolution of Dark Sector

- If a theory is thermally decoupled from the SM, it may have a different temperature
- Total entropy in dark and SM sector will be conserved
- Ratios of entropies densities are then constant:

$$\text{const} = \frac{s_d}{s_{\text{SM}}} = \frac{h_d(T_d)T_d^3}{h_{\text{SM}}(T_{\text{SM}})T_{\text{SM}}^3}$$

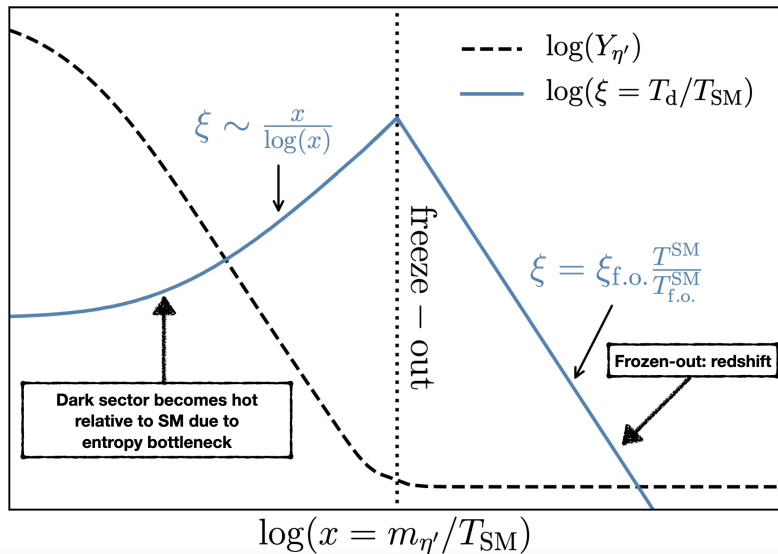
- We can determine dark temperature at late times if we know ratio at some early time

$$\xi(T_{\text{SM}}) \equiv \frac{T_d}{T_{\text{SM}}} = \left( \frac{h_{\text{SM}}}{h_{\text{SM}}^\infty} \frac{h_d^\infty}{h_d(\xi T_{\text{SM}})} \right)^{1/3} \xi^\infty$$

- As long as dark sector is in thermal equilibrium, it becomes exponentially hot relative to SM bath

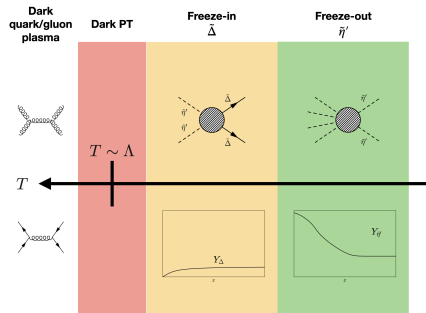
$$h(x = m/T) \sim x^3 K_3(x) \sim x^{5/2} x^{-x}, \quad (x \rightarrow \infty)$$

# Thermal Evolution of Dark Sector



# Cosmic Evolution

- ① High temperatures: dark quark-gluon plasma
- ②  $T \sim \Lambda$ : dark quark and gluons confine to  $\tilde{\eta}'$  and  $\tilde{\Delta}$
- ③  $n_{\Delta}$  initially suppress due to difficulty in forming
- ④  $\tilde{\Delta}$ s are frozen in via  $2\tilde{\eta}' \rightarrow \tilde{\Delta}\tilde{\Delta}$
- ⑤  $\tilde{\eta}'$  annihilate via  $4\tilde{\eta}' \rightarrow 2\tilde{\eta}'$



# Experimental Handels

- Measurements from bullet cluster and shapes of halos put tight constraints on self-interaction cross section

$$\sigma_{\text{SI}} \lesssim \frac{\text{barn}}{\text{GeV}}$$

- BBN and CMB constrain the effective number of neutrino constraints:

$$\Delta N_{\text{eff}} < 0.3$$

- If the  $\tilde{\eta}'$  is in equilibrium for too long, we affect  $N_{\text{eff}}$

$$N_{\text{eff}}^{\text{CMB}} \sim 3.046 + \frac{4}{7} \left( \frac{11}{4} \right)^{4/3} g_d^{\text{CMB}} \xi_{\text{CMB}}^4, \quad N_{\text{eff}}^{\text{BBN}} \sim 3 + \frac{4}{7} g_d^{\text{BBN}} \xi_{\text{BBN}}^4$$



# Relic Densities

- $\tilde{\eta}'$  relic density can be approximated using entropy conservation and instantaneous freeze-out

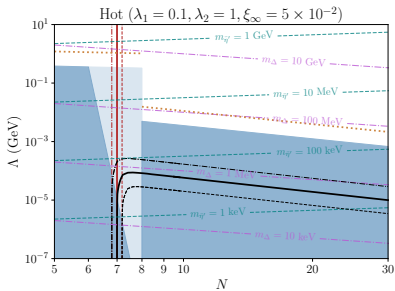
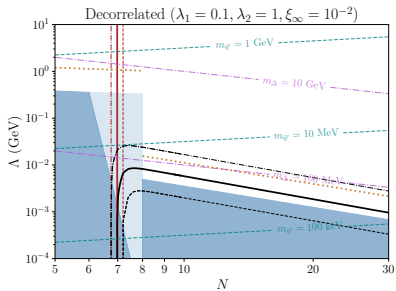
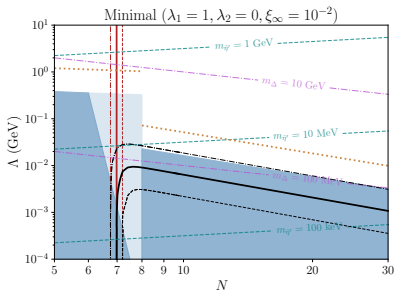
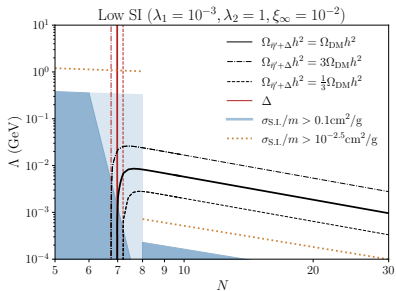
$$r_s = \frac{h_d}{h_{\text{SM}}} \xi^3 \sim \frac{N^2}{100} \xi_{\infty}^3, \quad Y_{\tilde{\eta}'} \sim \frac{n_{\tilde{\eta}'}}{s_{\text{SM}}} = \frac{r_s}{x^{d,f}}$$

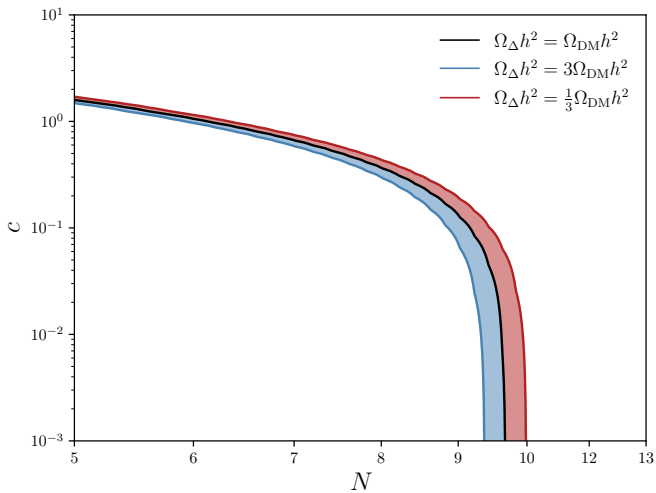
- Putting together:

$$\Omega_{\tilde{\eta}'} h^2 \sim 0.12 \left( \frac{10}{x_{d,f} + 1} \right) \left( \frac{\xi_{\infty}}{10^{-2}} \right)^3 \left( \frac{\Lambda}{20 \text{ MeV}} \right) \left( \frac{N}{10} \right)^{3/2}$$

- $\tilde{\Delta}$  relic density from direct integration of Boltzmann equation:

$$\Omega_{\tilde{\Delta}} h^2 \sim (\text{const.}) N^{3/2} e^{-2(c+1)N}$$





# One-Loop Charge-Breaking Minima in the Two-Higgs Doublet Model

Pedro Ferreira, Stefano Profumo, **LM**:  
arXiv:1910.08662

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- Possible to show that tree-level THDM potential with softly broken  $\mathbb{Z}_2$  yields either an EW or CB minimum, **but not both**

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$$\text{EW :} \quad \langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_1 \end{pmatrix}, \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 \end{pmatrix}$$

$$\text{CB :} \quad \langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} \alpha \\ \bar{v}_1 \end{pmatrix}, \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \bar{v}_2 \end{pmatrix}$$



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- Does this hold at 1-loop?

# One-Loop Corrections

- One-loop corrections are included using the effective potential:

$$V_{\text{eff}}(\bar{\phi}) = V_{\text{tree}}(\bar{\phi}) + \frac{\hbar}{64\pi^2} \sum_i (-1)^{2s_i} n_i [M_i^2(\bar{\phi})]^2 \left[ \log\left(\frac{M_i^2(\bar{\phi})}{\mu^2}\right) - c_i \right]$$

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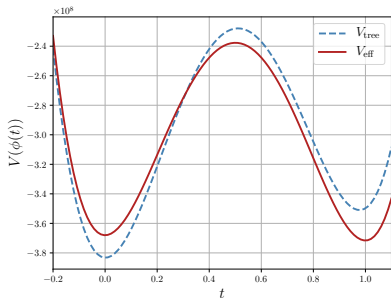
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- **Results: there exists parameters with simultaneous CB and EW minima**
- Tend to occur when  $V_{\text{CB}} \sim V_{\text{EW}}$

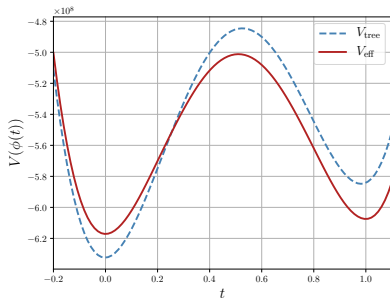
# One dimensional slices of the effective scalar potential

$$\phi(t) = (1 - t)\phi_{\text{EW}} + t\phi_{\text{CB}}$$

$$\phi(0) = \phi_{\text{EW}}, \quad \phi(1) = \phi_{\text{CB}}$$

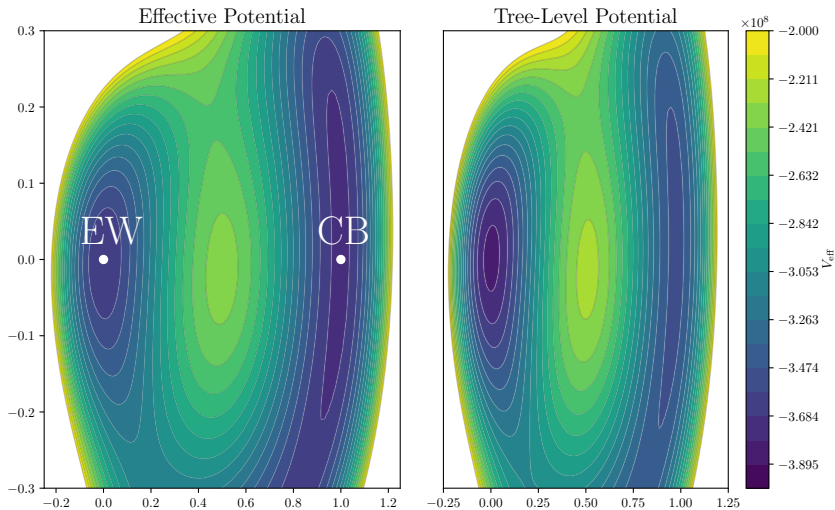


(a)  $V_{\text{eff}}(\phi_{\text{EW}}) < V_{\text{eff}}(\phi_{\text{CB}})$

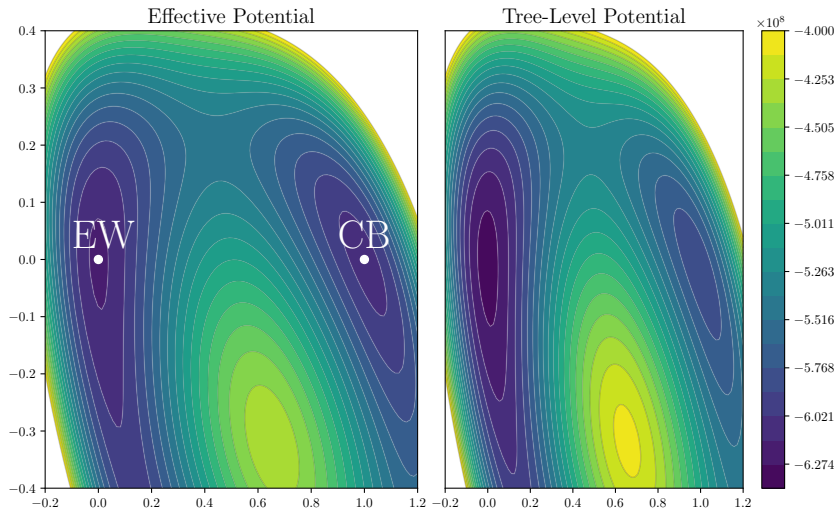


(b)  $V_{\text{eff}}(\phi_{\text{CB}}) < V_{\text{eff}}(\phi_{\text{EW}})$

$$V_{\text{eff}}(\phi_{CB}) < V_{\text{eff}}(\phi_{EW})$$



$$V_{\text{eff}}(\phi_{EW}) < V_{\text{eff}}(\phi_{CB})$$





# Asymptotic analysis of the Boltzmann equation for dark matter relic abundance

Hiren H. Patel, Jaryd F. Ulbricht, **LM**:  
arXiv:2009.04012

# Asymptotic Analysis of the Boltzmann Equation

- ① Dark Matter relic abundance determined using first moment of Boltzmann equation

$$\frac{dY}{dx} = -\lambda f(x) \left[ Y^2 - Y_{\text{eq}} \right],$$
$$\lambda f(x) = \sqrt{\frac{\pi}{45}} \frac{m_\chi M_{\text{pl}}}{x^2} \frac{h}{\sqrt{g}} \left( 1 + \frac{1}{3h} \frac{dh}{dx} \right) \langle \sigma v_{\text{Mø1}} \rangle$$

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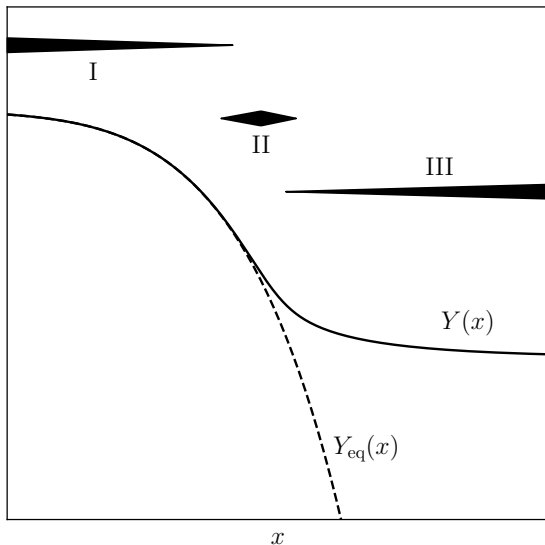
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- ④ Asymptotic analysis gives method for arbitrary accurate results with error estimates

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